

## Subject card

| Subject name and code                       | Numerical Methods, PG_00159207  |  |   |                                     |        |                   |         |     |
|---|---|--|---|-------------------------------------|--------|-------------------|---------|-----|
| Field of study                              | Quantum Information Technology  |  |   |                                     |        |                   |         |     |
| Date of commencement of studies             | October 2024  |  | Academic year of realisation of subject |                                     |        | 2025/2026         |         |     |
| Education level                             | Master's studies  |  | Subject group                           |                                     |        |                   |         |     |
| Mode of study                               | full-time studies   |  | Mode of delivery                        |                                     |        | at the university |         |     |
| Year of study                               | 2   |  | Language of instruction                 |                                     |        | English           |         |     |
| Semester of study                           | 3   |  | ECTS credits                            |                                     | 6.0    |                   |         |     |
| Learning profile                            | academic  | Assessment form  |   |                                     |        |                   |         |     |
| Conducting unit                             | Faculty of Mathematics, Physics and Informatics -> Rector   |  |   |                                     |        |                   |         |     |
| Name and surname                            | Subject supervisor  |  | dr inż. Piotr Mironowicz                |                                     |        |                   |         |     |
| of lecturer (lecturers)                     | Teachers  |  |   |                                     |        |                   |         |     |
| Lesson types                                | Lesson type   | Lecture  | Tutorial                                | Laboratory                          | Projec | t                 | Seminar | SUM |
|   | Number of study<br>hours  | 30.0   | 30.0                                    | 0.0                                 | 0.0    |                   | 0.0     | 60  |
|   | E-learning hours included: 0.0  |  |   |                                     |        |                   |         |     |
| Learning activity and number of study hours | Learning activity   | Participation in didactic<br>classes included in study<br>plan |   | Participation in consultation hours |        | Self-study        |         | SUM |
|   | Number of study<br>hours  | 60   |   | 0.0                                 |        | 30.0              |         | 90  |
| Subject objectives                          | This course is an advanced course of numerical methods for quantum information. To explore quantum information one require computational methods since mathematical models are only rarely solvable algebraically. Numerical methods, based upon computational mathematics and quantum physics, are the basic algorithms enabling computer predictions in quantum information. Such methods include techniques for optimization, linear algebra underlying eigenvalue problem, stochastic simulation. |  |   |                                     |        |                   |         |     |

| Learning outcomes | Course outcome  | Subject outcome   | Method of verification   |  |  |  |  |
|-------------------|---|---|--|--|--|--|--|
|                   | [QITL3_U05] has the ability to<br>synthesize methods and ideas<br>from various areas of physics and<br>other branches of science; is able<br>to notice that distant phenomena<br>are sometimes described by<br>similar models   | Student has the ability to connect<br>analytical methods of open<br>quantum systems and techniques<br>for their numerical simmulation<br>with tools used in different areas<br>of physics | [SU4] test/exam - oral or written<br>[SU5] implementation of a<br>problem task |  |  |  |  |
|                   | [QITL3_W03] knows advanced<br>experimental, observational and<br>numerical techniques allowing to<br>plan and perform a complex<br>physical experiment or computer<br>simulation  | Student knows how to do<br>numerical calculations and<br>simulations to solve many-body<br>differential equations.  | [SW4] test/exam - oral or written<br>[SW5] implementation of a<br>problem task |  |  |  |  |
|                   | [QITL3_W06] has knowledge of<br>current directions in the<br>development of physics, in<br>particular in the field of quantum<br>information theory   | Student knows about newest developments in numerical optimization methods.  | [SW4] test/exam - oral or written<br>[SW5] implementation of a<br>problem task |  |  |  |  |
|                   | [QITL3_W05] knows the<br>theoretical foundations of<br>computational methods and IT<br>techniques used to model and<br>simulate physical systems<br>considered in quantum information<br>theory   | Student knows stochastic<br>simmulation methods and<br>understands their rationale.   | [SW4] test/exam - oral or written<br>[SW5] implementation of a<br>problem task |  |  |  |  |
|                   | [QITL3_W02] has in-depth<br>knowledge in the field of advanced<br>mathematics and mathematical<br>and computer methods, necessary<br>to solve physical problems of<br>medium complexity, and<br>advanced knowledge in the area<br>of quantum information and its<br>technological aspects | Student knows methods used to simulate many-body systems.   | [SW4] test/exam - oral or written<br>[SW5] implementation of a<br>problem task |  |  |  |  |
| Subject contents  | Optimization: basic concepts, compu   |   |  |  |  |  |  |
|                   | Linear programming: simplex method, duality and sensitivity.<br>Unconstrained optimization: method of steepest descent, Newtons method, conjugate gradient algorithm;<br>linear least squares, robust optimization.   |   |  |  |  |  |  |
|                   | Constrained optimization: projected gradient methods; sequential unconstrained minimization, convex optimization, nonlinear optimization.   |   |  |  |  |  |  |
|                   | Combinatorial optimization: simulated annealing.  |   |  |  |  |  |  |
|                   | Maximum likelihood estimation.  |   |  |  |  |  |  |
|                   | Evolutionary algorithm.   |   |  |  |  |  |  |
|                   | Singular value decomposition, the pseudo-inverse.   |   |  |  |  |  |  |
|                   | Matrix eigenvalues: Jacobis method, Givens transformation, Householder transformation, the LR method, the QR method.  |   |  |  |  |  |  |
|                   | Maximum (minimum) modulus eigenvalue: power method, inverse power iteration, shifted inverse power iteration.   |   |  |  |  |  |  |
|                   | The general eigenvalue problem.   |   |  |  |  |  |  |
|                   | Numerical methods for sampling from a given density Numerical simulations of master equations.  |   |  |  |  |  |  |
|                   | Software for optimization, eigenproblem solution and stochastic simulations.  |   |  |  |  |  |  |

| Prerequisites<br>and co-requisites                             | Passing Programming course at semester 1. |   |                               |  |  |  |
|--|---|---|-------------------------------|--|--|--|
| Assessment methods   | Subject passing criteria                  | Passing threshold   | Percentage of the final grade |  |  |  |
| and criteria   | tutorial part: test                       | 51.0%   | 50.0%                         |  |  |  |
|  | lecture part: exam                        | 51.0%   | 50.0%                         |  |  |  |
| Recommended reading  | Basic literature                          | G. S. Chirikjian, Stochastic Models, Information Theory, Analytic<br>Methods and Modern Applications and Lie Groups,Vol. 2, Analytic<br>Methods and |                               |  |  |  |
|  |   | Modern Applications, Springer Science+Business Media, 2012  |                               |  |  |  |
|  |   | S. Butenko, P.M. Pardalos, Numerical Methods and Optimization, An Introduction, Taylor & Francis Group 1014   |                               |  |  |  |
|  |   | S. K. Bose, Numerical Methods of Mathematics Implemented in Fortran, Springer Nature Singapore Pte Ltd. 2019  |                               |  |  |  |
|  |   | A. Kharab, R. B. Guenther, An Introduction to Numerical Methods, A<br>MATLAB Approach, Taylor & Francis Group, 2019                                 |                               |  |  |  |
|  |   | É. Walter, Numerical Methods and Optimization, A Consumer Guide, Springer International Publishing Switzerland 2014                                 |                               |  |  |  |
|  |   | G. Lindfield, J. Penny, Numerical Methods Using MATLAB, Elsevier 2019   |                               |  |  |  |
|  |   | R. Toral, P. Colet, Stochastic Numerical Methods, An Introduction for Students and Scientists, Wiley-VCH 2014                                       |                               |  |  |  |
|  |   | R. K. Gupta, Numerical Methods Fundamentals and Applications,<br>Cambridge University Press 2019  |                               |  |  |  |
|  |   |   |                               |  |  |  |
|  |   |   |                               |  |  |  |
|  | Supplementary literature                  | None.   |                               |  |  |  |
|  | ekesources addresses                      | Adresy na platformie eNauczanie:  |                               |  |  |  |
| Example issues/<br>example questions/<br>tasks being completed |   |   |                               |  |  |  |
| Work placement   | Not applicable                            |   |                               |  |  |  |

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